

NANO EXPRESS

Open Access

Microwave-induced resistance oscillations and zero resistance states in 2D bilayer systems

Jesus Iñarrea

Abstract

We report on theoretical studies of recently obtained experimental results on microwave-induced resistance oscillations and zero resistance states in Hall bars with two occupied subbands. In these experiments, resistance presents a peculiar shape which appears to have a built-in interference effect not observed before. We apply the microwave-driven electron orbit model, which implies a radiation-driven oscillation of the two-dimensional electron system. Thus, we calculate different intra- and inter-subband electron scattering rates revealing different microwave-driven oscillations frequencies for the two electronic subbands. Calculated results are in good agreement with experiments.

Keywords: Bilayer systems, Microwaves, Magnetoresistance

Background

In the last decade, it was discovered that when a Hall bar (a 2DES with a uniform and perpendicular magnetic field (B)) is irradiated with microwaves, some unexpected effects are revealed, deserving special attention from the condensed matter community: microwave-induced (MW) resistance oscillations (MIRO) and zero resistance states (ZRS) [1,2]. Different theories have been proposed to explain these striking effects [3-9] but the physical origin is still being questioned. On the other hand, a great effort has been made, specially from the experimental side, growing better samples, adding new features and different probes to the basic experimental setup, etc. [10-16]. One of the most interesting setups, carried out recently, consists in using samples with two or three occupied subbands [15]. These samples are either based in a double-quantum-well structure or just one single but wide quantum well.

The main difference in the longitudinal magnetoresistance (R_{xx}) of a two-subband sample is the presence of magneto-intersubband oscillations (MISO) [17,18]. These oscillations occur due to periodic modulation of the probability of transitions through elastic scattering between Landau levels of different subbands [19-22]. Under MW irradiation, the first experimental results

[16] of R_{xx} showed the interference of MISO and MIRO without reaching the ZRS regime. Later on, further experiments realized at higher MW intensities and mobility samples showed that the MW-response evolves into zero-resistance states for the first time in a two-occupied subband sample [15]. In the same experiment [15], it was also observed that there is a peculiar R_{xx} profile with different features regarding the one-subband case [1,2] affecting only valleys and peaks of MIRO's in a surprising regular way, deserving special attention.

In this letter, we theoretically study magnetoresistance of a Hall bar being illuminated with MW radiation when two electronic subbands participate in the transport. We apply the theory developed by the authors, the *MW-driven electron orbits model* [3,23,24], which we extend to a two-subband scenario. According to this theory [3], when a Hall bar is illuminated, the electron orbit centers of the Landau states perform a classical trajectory consisting in a harmonic motion along the direction of the current (see ref. [3] for a detailed explanation).

In a double subband scenario, the situation gets more complicated but with a richer physics. On the one hand, due to the presence of MW, we have two 2DES (two subbands) moving harmonically at the MW frequency. On the other hand, we have two possible scattering processes with charged impurities: intra- and inter-subbands.

The competition between intra- and inter-subband scattering events under the presence of radiation alters

Correspondence: jinarrea@fis.uc3m.es
Escuela Politécnica Superior, Universidad Carlos III, Leganes, Madrid, 28911, Spain

significantly the transport properties of the sample. This is reflected in the R_{xx} profile through a strong and peculiar interference effect. As in experiments, our calculated results recover the presence of new features regularly spaced through the whole MIRO's profile, mainly two shoulders at minima and narrower peaks.

Methods

The MW driven electron orbits model, was developed to explain the R_{xx} response of an irradiated 2DEG at low B . We first obtained the exact solution of the corresponding electronic wave function [3,23-29]:

$\Psi_N(x, t) \propto \phi_n(x - X - x_{cl}(t), t)$, where ϕ_n is the solution for the Schrödinger equation of the unforced quantum harmonic oscillator, X is the center of the electron orbit. $x_{cl}(t)$ is the classical solution of a forced and damped harmonic oscillator [3-6,23,24]; $x_{cl} = \frac{eE_0}{m^* \sqrt{(w_c^2 - w^2)^2 + \gamma^4}} \cos wt = A \cos wt$, where γ is a phenomenologically-introduced damping factor for the electronic interaction with acoustic phonons, E_0 is the amplitude of the MW-electric field, and w is the frequency of MW.

Thus, the electron orbit centers are not fixed, but they oscillate harmonically at w . This *radiation-driven* behavior will dramatically affect the charged impurity scattering and eventually the conductivity. Thus, we introduce the scattering suffered by the electrons due to charged impurities. If the scattering is weak, we can apply a time-dependent first-order perturbation theory. First, we calculate the impurity scattering rate [3-6,23,30] between two *oscillating* Landau states Ψ_N and Ψ_M belonging to the same subband, i.e., the intra-subband scattering rate $W_{n,m}^{intra}$ and to different subband, i.e., the inter-subband $W_{n,m}^{inter}$:

$$W_{n,m}^{intra} = |F_{intra}|^2 \frac{e^5 N_i B m^*}{\hbar^2 \epsilon^2 q_0^2} \left[1 + 2 \sum_{s=1}^{\infty} e^{\left(\frac{-s\pi\Gamma}{\hbar w_c}\right)} \right], \quad (1)$$

$$W_{n,m}^{inter} = |F_{inter}|^2 \frac{e^5 N_i B m^*}{\hbar^2 \epsilon^2 q_0^2} \times \left[1 + 2 \sum_{s=1}^{\infty} e^{\left(\frac{-s\pi\Gamma}{\hbar w_c}\right)} \cos\left(\frac{s2\pi\Delta_{12}}{\hbar w_c}\right) \right], \quad (2)$$

ϵ being the dielectric constant, N_i the number of impurities, Γ the width of the Landau states, Δ_{12} the subband separation, and q_0 as the Thomas-Fermi screening constant [31]. F_{intra} and F_{inter} are the form factors given by:

$$F_{intra(inter)} = \int_0^{\infty} e^{-q(z-z_i)} \Psi_S^* \Psi_{S(A)} dz = \frac{e^{-qd}}{2} \left[\left(\frac{b}{b+q}\right)^3 + (-) \left(\frac{b}{b-q}\right)^3 \right]. \quad (3)$$

To obtain the form factor expressions, we have considered at each side of the wide quantum well a triangular shape potential. Thus, we have applied the Fang-Howard approach (see ref. [31]) for the electronic wave function, where b is a variational parameter, and q is the electron wave vector exchanged in the scattering. $\Psi_{S(A)}$ are the corresponding symmetric (antisymmetric) wave function of the wide quantum well. We have supposed a symmetrical delta doping, d being the average separation between the impurities and the 2DES at each side of the wide quantum well. With the experimental parameters at hand [15] and following the variational approach [31], we have carried out the calculation of the relative values of F_{intra} and F_{inter} resulting in $|F_{intra}|^2 \simeq 3 \times |F_{inter}|^2$. Next, we find the average effective distance advanced by the electron in every scattering jump, ΔX^{MW} .

Results and discussion

If we consider that the oscillation is at its *mid-point* when the electron jumps from the initial state and that it takes an average time $\langle \tau_{intra(inter)} \rangle = \langle 1/W_{n,m}^{intra(inter)} \rangle$ to get to the final one, then we can write for the average coordinate change in the x direction: $\Delta X_{intra(inter)}^{MW} = \Delta X^0 + A \cos(w \langle \tau_{intra(inter)} \rangle)$, where ΔX^0 is the effective distance advanced when there is no MW field present.

Then, we calculate average values of the intra and inter-subband scattering rates and obtain a direct relationship given by $\langle W_{n,m}^{intra} \rangle \approx 3 \times \langle W_{n,m}^{inter} \rangle \Rightarrow \langle \tau_{intra} \rangle \approx \frac{1}{3} \langle \tau_{inter} \rangle$, where we have considered that the cosine average value, $\left\langle \cos \frac{s2\pi\Delta_{12}}{\hbar w_c} \right\rangle \rightarrow 0$ for $\Delta_{12} > \hbar w_c$, and we have carried out the sum $\sum_{s=1}^{\infty} e^{\left(\frac{-s\pi\Gamma}{\hbar w_c}\right)} \rightarrow \frac{\exp\left(\frac{-s\pi\Gamma}{\hbar w_c}\right)}{1 - \exp\left(\frac{-s\pi\Gamma}{\hbar w_c}\right)}$. We have taken an average value for the variational parameter $\bar{b} = 0.3 \text{ nm}^{-1}$, meaning an average width for the two lateral triangular shape wells of $\langle z \rangle = 10-12 \text{ nm}$ [31].

$$\sigma_{xx} = \frac{6e^7 m^{*2} B N_i}{\pi \epsilon^2 \hbar^6 q_0} \left[\Delta X^0 + A \cos \frac{1}{3} w \langle \tau_{inter} \rangle \right]^2 \times \left[1 + 2e^{\frac{-\pi\Gamma}{\hbar w_c}} + e^{\frac{-\pi\Gamma}{\hbar w_c}} \frac{X_S}{\sinh X_S} \left(\cos \frac{2\pi(E_F - E_1)}{\hbar w_c} + \cos \frac{2\pi(E_F - E_2)}{\hbar w_c} \right) \right] + \frac{2e^7 m^{*2} B N_i}{\pi \epsilon^2 \hbar^6 q_0} \left[\Delta X^0 + A \cos w \langle \tau_{inter} \rangle \right]^2 \times \left[1 + 2e^{\frac{-\pi\Gamma}{\hbar w_c}} \cos \frac{2\pi\Delta_{12}}{\hbar w_c} + e^{\frac{-\pi\Gamma}{\hbar w_c}} \frac{X_S}{\sinh X_S} \left(\cos \frac{2\pi(E_F - E_1)}{\hbar w_c} + \cos \frac{2\pi(E_F - E_2)}{\hbar w_c} \right) \right], \quad (4)$$

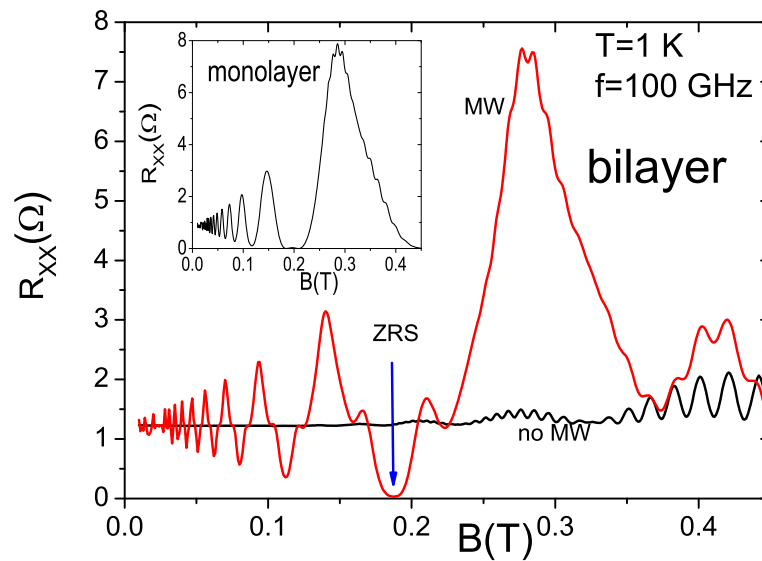


Figure 1 Calculated R_{xx} vs B for dark (no MW) and MW situations. The ZRS is marked with an arrow. The MW frequency is 100 GHz. We observe clearly the peculiar features for bilayer systems: shoulders at minima and narrower peaks regarding the single occupied subband case (see inset). Shoulders and narrow peaks are the outcomes of the interference between the intra- and inter-subband scattering processes.

where $X_S = \frac{2\pi^2 k_B T}{\hbar w_c}$ and E_1 and E_2 are the energies of the first and the second subbands, respectively. This equation shows the physical equivalence to a situation with only one scattering time and two different oscillations frequencies for the MW-driven subbands: $w/3$ for the intra-subband and w for the inter-subband scattering rate [32,33]. They demonstrate also the origin for the regular and strong interference profile observed in experiments where the factor $1/3$ is essential to obtain the interference effect regularly spaced affecting only valleys and peaks. A different factor would produce a totally distinct interference and also distinct R_{xx} response. This factor comes from the calculation of the squared magnitude of the corresponding form factors which eventually determine the different scattering rates between the intra-subband and the inter-subband processes.

In physical terms, during the scattering jump, the electron *perceives* approximately three times faster MW-driven oscillation of the 2DES when is inter-subband with respect to the intra-subband. Then, we are going to obtain a MIRO profile made up of two different MW frequencies, as if the sample was illuminated by two different radiation sources at the same time. This gives rise to a clear interference effect reflected in the final R_{xx} profile. To obtain R_{xx} , we use the relation $R_{xx} = \frac{\sigma_{xx}^2}{\sigma_{xx}^2 + \sigma_{xy}^2} \simeq \frac{\sigma_{xx}^2}{\sigma_{xy}^2}$, where $\sigma_{xy} \simeq \frac{\hbar e}{B}$ and $\sigma_{xx} \ll \sigma_{xy}$.

In Figure 1, we present calculated R_{xx} vs B for dark and MW situations and frequency $f = w/2\pi = 100$ GHz. We can observe MISO peaks for the dark curve, MIRO for the MW curve, and the ZRS marked with an arrow.

We observe the new features appearing regularly spaced in peaks and valleys for bilayer systems: two nearly symmetric shoulders in valleys and narrower peaks with respect to the single occupied subband case (see inset). According to our model, these new features are results of the interference between the competing intra- and inter-subband scattering processes. In valleys, we observe a constructive interference effect giving rise to two shoulders, meaning more current through the sample; meanwhile, the narrower peaks mean a destructive interference and less current.

Conclusions

In summary, we have theoretically studied the recently discovered microwave-induced resistance oscillations and zero resistance states in Hall bars with bilayer systems. Resistance presents a peculiar shape which appears to have an interference effect not observed before. Applying the microwave-driven electron orbit model, we calculate different intra- and inter-subband electron scattering rates under MW, revealing that the former is three times greater than the latter. This is physically equivalent to different microwave-driven oscillation frequencies for the two electronic subbands.

Competing interests

The author has no competing interests.

Acknowledgements

This work is supported by the MICYT (Spain) under grant MAT2011-24331 and by the ITN grant 234970 (EU).

Received: 9 November 2012 Accepted: 3 April 2013
Published: 29 May 2013

References

1. Mani RG, Smet JH, von Klitzing K, Narayanamurti V, Johnson WB, Umansky V: **Zero-resistance states induced by electromagnetic-wave excitation in GaAs/AlGaAs heterostructures.** *Nature* (London) 2002, **420**:646–650.
2. Zudov MA, Du RR, Pfeiffer LN, West KW: **Evidence for a new dissipationless effect in 2D electronic transport.** *Phys Rev Lett* 2003, **90**:046807.
3. Iñarrea J, Platero G: **Theoretical approach to microwave-radiation-induced zero-resistance states in 2D electron systems.** *Phys Rev Lett* 2005, **94**:016806.
4. Iñarrea J, Platero G: **From zero resistance states to absolute negative conductivity in microwave irradiated two-dimensional electron systems.** *Appl Phys Lett* 2006, **89**:052109.
5. Iñarrea J, Platero G: **Polarization immunity of magnetoresistivity response under microwave excitation.** *Phys Rev B* 2007, **76**:073311.
6. Iñarrea J: **Hall magnetoresistivity response under microwave excitation revisited.** *Appl Phys Lett* 2007, **90**:172118.
7. Durst AC, Sachdev S, Read N, Girvin SM: **Radiation-induced magnetoresistance oscillations in a 2D electron gas.** *Phys Rev Lett* 2003, **91**:086803.
8. Lei XL, Liu SY: **Radiation-induced magnetoresistance oscillation in a two-dimensional electron gas in Faraday geometry.** *Phys Rev Lett* 2003, **91**:226805.
9. Rivera PH, Schulz PA: **Radiation-induced zero-resistance states: Possible dressed electronic structure effects.** *Phys Rev B* 2004, **70**:075314.
10. Mani RG, Smet JH, von Klitzing K, Narayanamurti V, Johnson WB, Umansky V: **Demonstration of a 1/4-Cycle phase shift in the radiation-induced oscillatory magnetoresistance in GaAs/AlGaAs devices.** *Phys Rev Lett* 2004, **92**:146801.
11. Mani RG, Smet JH, von Klitzing K, Narayanamurti V, Johnson WB, Umansky V: **Radiation-induced oscillatory magnetoresistance as a sensitive probe of the zero-field spin-splitting in high-mobility GaAs/AlGaAs devices.** *Phys Rev B* 2004, **69**:193304.
12. Mani RG: **Zero-resistance states induced by electromagnetic-wave excitation in GaAs/AlGaAs heterostructures.** *Physica E (Amsterdam)* 2004, **22**:1.
13. Mani RG, Johnson WB, Umansky V, Narayanamurti V, K Ploog K: **Phase study of oscillatory resistances in microwave-irradiated- and dark-GaAs/AlGaAs devices: indications of an unfamiliar class of the integral quantum Hall effect.** *Phys Rev B* 2009, **79**:205320.
14. Mani RG, Gerl C, Schmult S, Wegscheider W, Umansky V: **Nonlinear growth in the amplitude of radiation-induced magnetoresistance oscillations.** *Phys Rev B* 2010, **81**:125320.
15. Wiedmann S, Gusev GM, Raichev OE, Bakarov AK, Portal JC: **Microwave zero-resistance states in a bilayer electron system.** *Phys Rev Lett* 2010, **105**:026804.
16. Wiedmann S, Gusev GM, Raichev OE, Bakarov AK, Portal JC: **Crossover between distinct mechanisms of microwave photoresistance in bilayer systems.** *Phys Rev B* 2010, **81**:085311.
17. Raichev OE: **Magnetic oscillations of resistivity and absorption of radiation in quantum wells with two populated subbands.** *Phys Rev B* 2008, **78**:125304.
18. Mamani NC, Gusev GM, Raichev OE, Lamas TE, Bakarov AK: **Nonlinear transport and oscillating magnetoresistance in double quantum wells.** *Phys Rev B* 2009, **80**:075308.
19. Mani RG: **Photo-excited zero-resistance states in the GaAs/AlGaAs system.** *Int J Mod Phys B* 2004, **18**:3473.
20. Mani RG: **Novel zero-resistance states induced by photoexcitation in the high mobility GaAs/AlGaAs two-dimensional electron system.** *Physica E* 2004, **25**:189.
21. Mani RG, Ramanayaka AN, Wegscheider W: **Observation of linear-polarization-sensitivity in the microwave-radiation-induced magnetoresistance oscillations.** *Phys Rev B* 2011, **84**:085308.
22. Mani RG, Hankinson J, Berger C, de Heer WA: **Observation of resistively detected hole spin resonance and zero-field pseudo-spin splitting in epitaxial graphene.** *Nature Comm* 2012, **3**:996.
23. Inarrea J, Platero G: **Magnetoresistivity modulated response in bichromatic microwave irradiated two dimensional electron systems.** *Appl Phys Lett* 2006, **89**:172114.
24. Kerner EH: **Note on the forced and damped oscillator in quantum mechanics.** *Can J Phys* 1958, **36**:371.
25. Iñarrea J, Platero G: **Driving Weiss oscillations to zero resistance states by microwave Radiation.** *Appl Phys Lett* 2008, **93**:062104.
26. Iñarrea J, Platero G: **Effect of an in-plane magnetic field on microwave-assisted magnetotransport in a two-dimensional electron system.** *Phys Rev B* 2008, **78**:193310.
27. Iñarrea J: **Effect of an in-plane magnetic field on microwave-assisted magnetotransport in a two-dimensional electron system.** *Appl Phys Lett* 2008, **92**:192113.
28. Inarrea J, Platero G: **Microwave magnetoabsorption in two-dimensional electron systems.** *Appl Phys Lett* 2008, **95**:162106.
29. Inarrea J, Platero G: **Electron-photon interaction in resonant tunneling diodes.** *Europhys Lett* 1997, **40**:417–422.
30. Ridley BK: *Quantum Processes in Semiconductors*. 4th ed. Oxford: Oxford University Press; 1993.
31. Ando T, Fowler A, Stern F: **Electronic properties of two-dimensional systems.** *Rev Mod Phys* 1982, **54**:437–672.
32. Inarrea J, Mani RG, Wegscheider W: **Sublinear radiation power dependence of photoexcited resistance oscillations in two-dimensional electron systems.** *Phys Rev B* 2010, **82**:205321.
33. Mani RG, Gerl C, Schmult S, Wegscheider W, Umansky V: **Nonlinear growth in the amplitude of radiation-induced magnetoresistance oscillations.** *Phys Rev B* 2010, **81**:125320.

doi:10.1186/1556-276X-8-259

Cite this article as: Iñarrea: Microwave-induced resistance oscillations and zero resistance states in 2D bilayer systems. *Nanoscale Research Letters* 2013 **8**:259.

Submit your manuscript to a SpringerOpen® journal and benefit from:

- Convenient online submission
- Rigorous peer review
- Immediate publication on acceptance
- Open access: articles freely available online
- High visibility within the field
- Retaining the copyright to your article

Submit your next manuscript at ► springeropen.com